

# **Measuring Altitude**

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# Techniques for measuring altitude

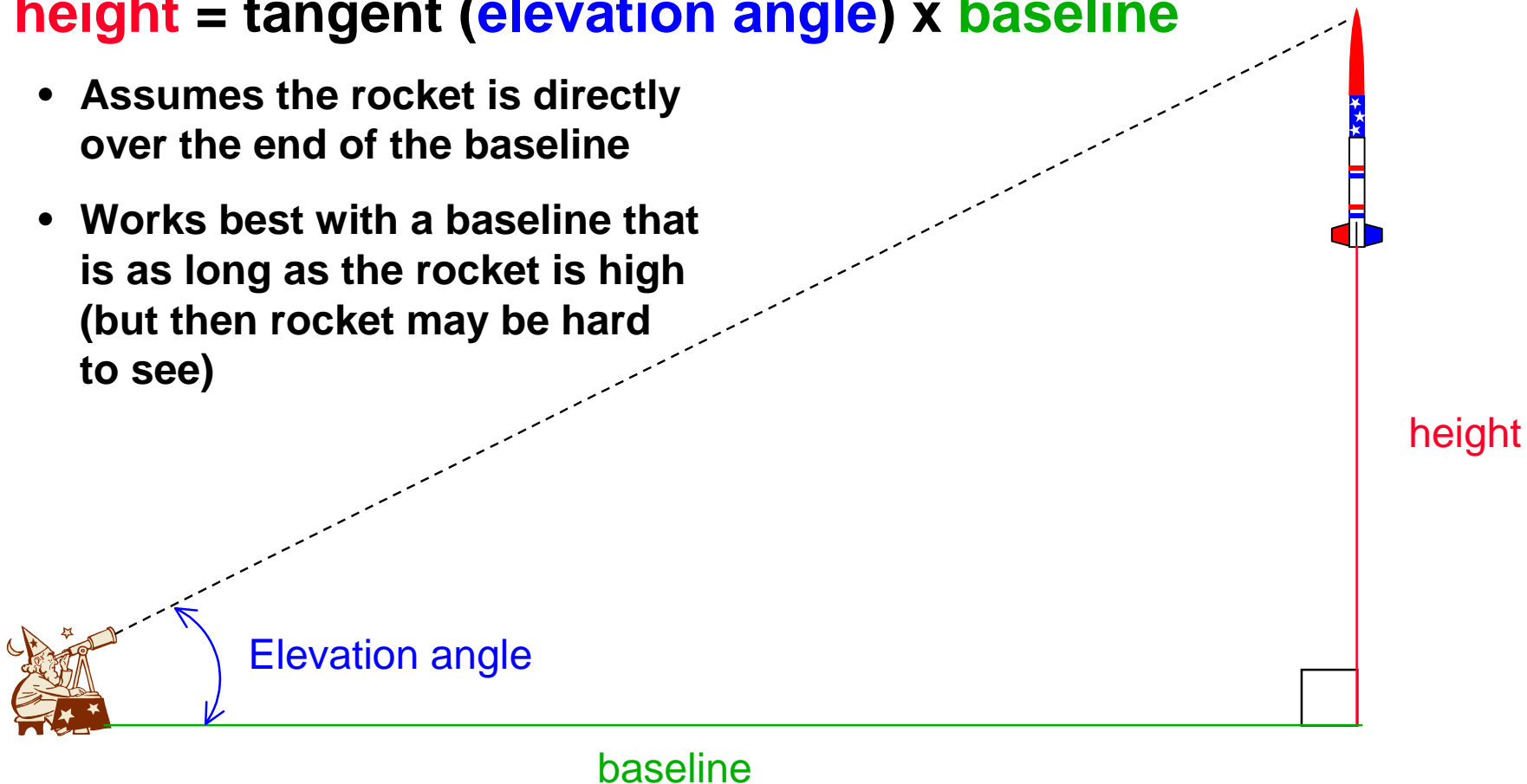
- **Dropping standard objects at apogee**
  - Ping pong balls
  - Standard weight and streamer combination
  - Can be accurate but hard to see
- **Altimeters**
  - Accelerometer
  - Barometric
  - Add weight and expense
- **Theodolites**
  - Single station
  - Multiple station
  - No change to the rocket
  - Still the gold standard for NAR

# Single station measurement

## Simple trigonometry:

**height** = tangent (**elevation angle**) x **baseline**

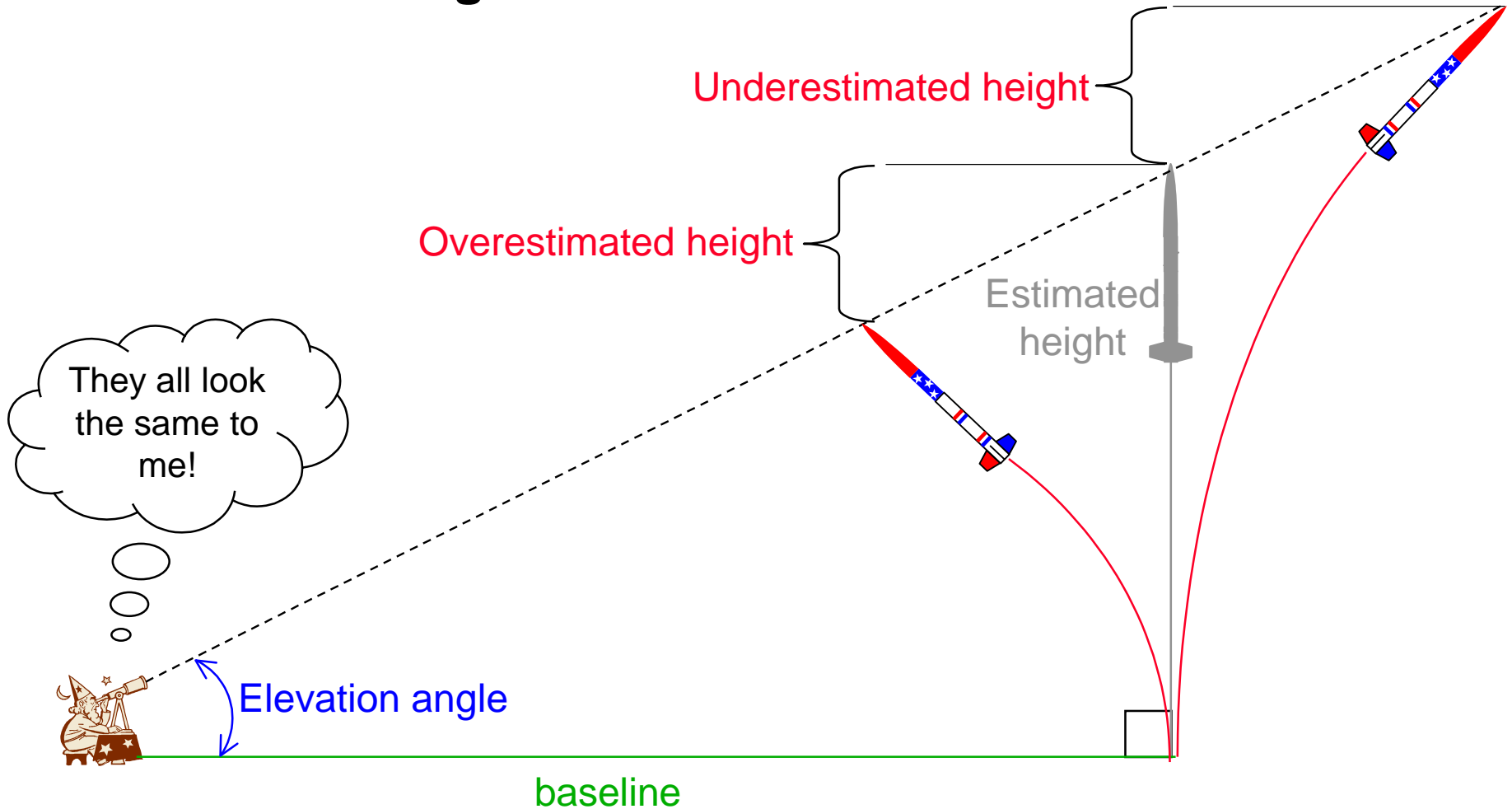
- Assumes the rocket is directly over the end of the baseline
- Works best with a baseline that is as long as the rocket is high (but then rocket may be hard to see)



**MASA**

# Single station measurement error

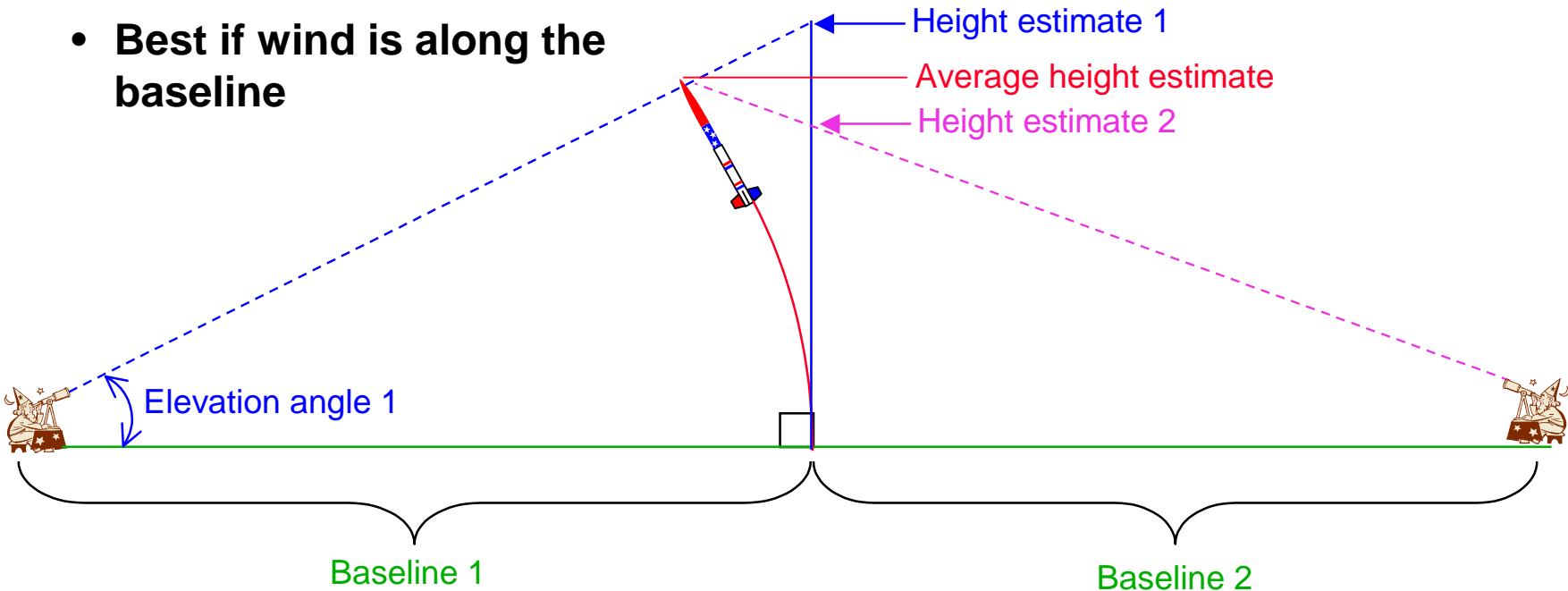
Weather cocking leads to errors!



# Single station error correction

## Additional stations can help, but increase the variability of the estimate

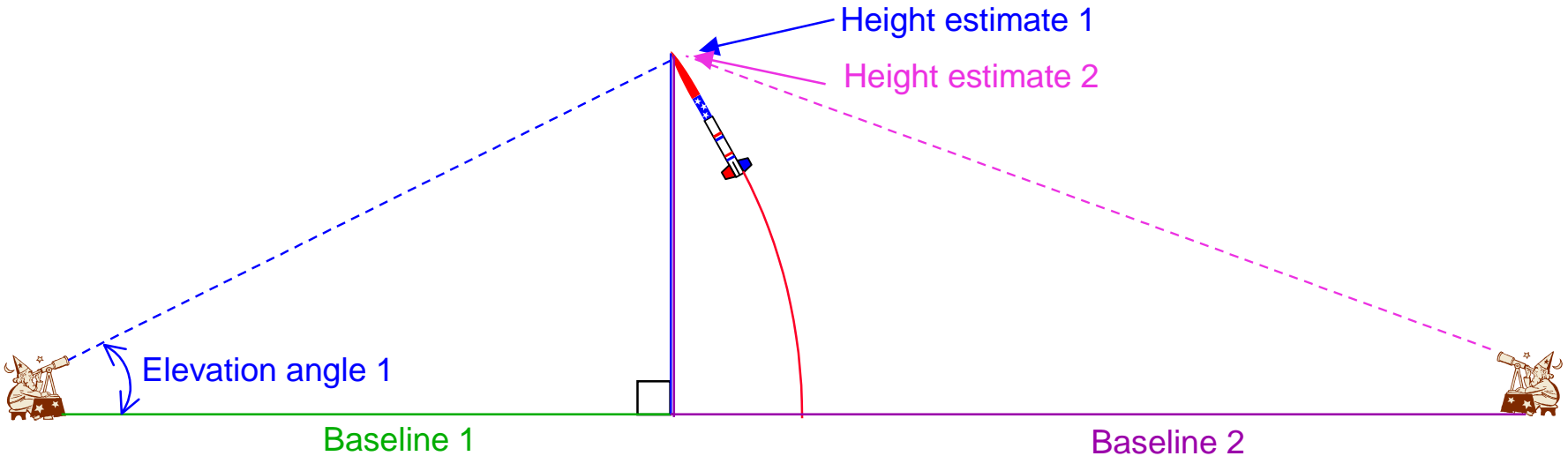
- Best if baselines are orthogonal
- Best if wind is along the baseline



# Need for multiple station measurement

## What if we knew the *real* baseline?

- Estimates would be very accurate!



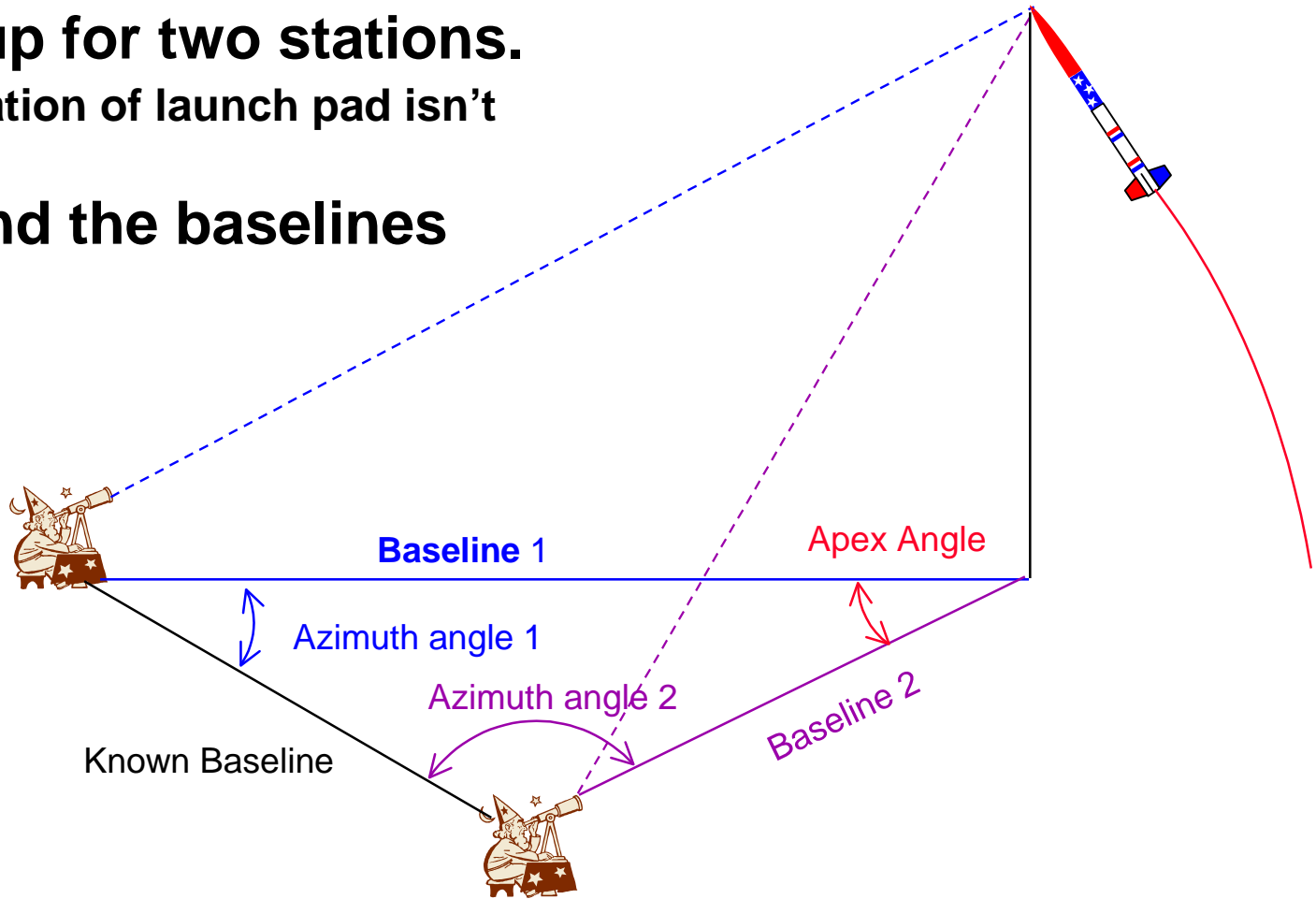
# Two station measurement

(One method)

## Basic set up for two stations.

(Note that location of launch pad isn't very relevant!)

## Step 1: Find the baselines



$$\text{Apex Angle} = 180 - \text{azimuth angle 1} - \text{azimuth angle 2}$$

$$\text{Baseline 1} = \text{known baseline} * \sin(\text{azimuth angle 2}) / \sin(\text{apex angle})$$

$$\text{Baseline 2} = \text{known baseline} * \sin(\text{azimuth angle 1}) / \sin(\text{apex angle})$$

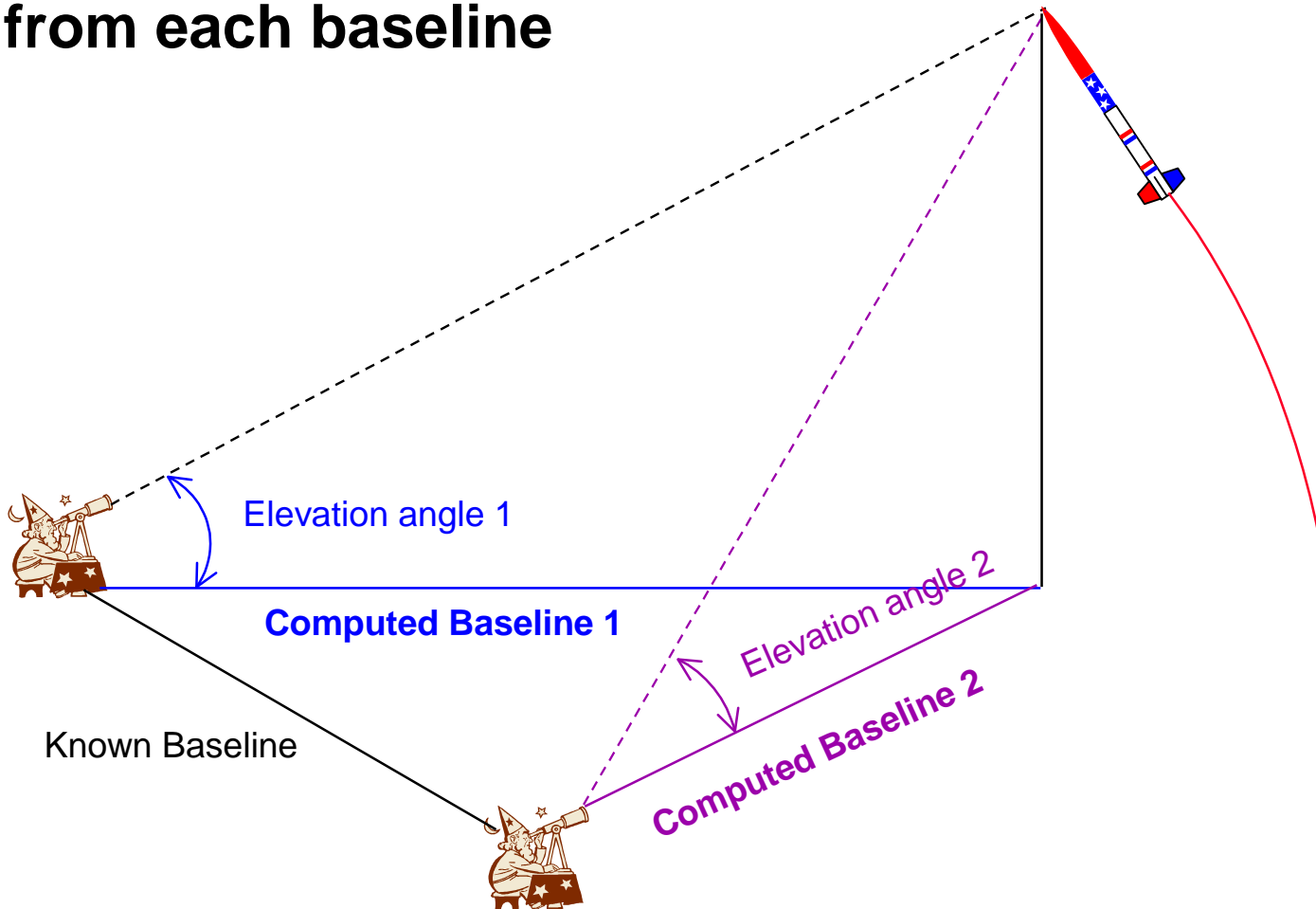
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# Two station measurement

**Step 2: Determine two estimates of altitude, one from each baseline**

$$\text{Estimate 1} = \text{Baseline 1} * \tan(\text{Elevation angle 1})$$

$$\text{Estimate 2} = \text{Baseline 2} * \tan(\text{Elevation angle 2})$$

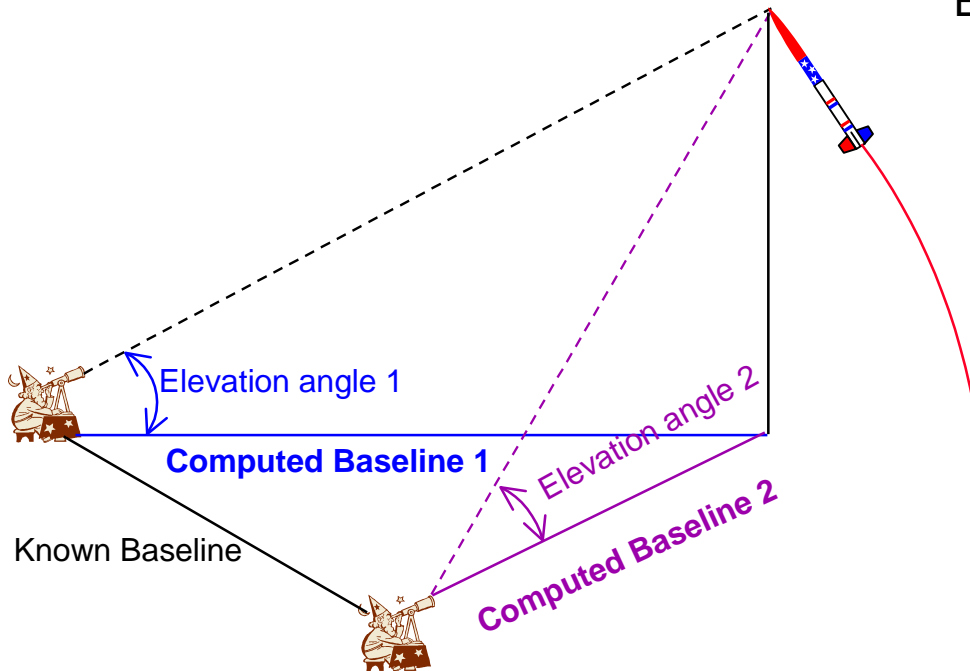




# Two station measurement

## Step 3: Compare two estimates

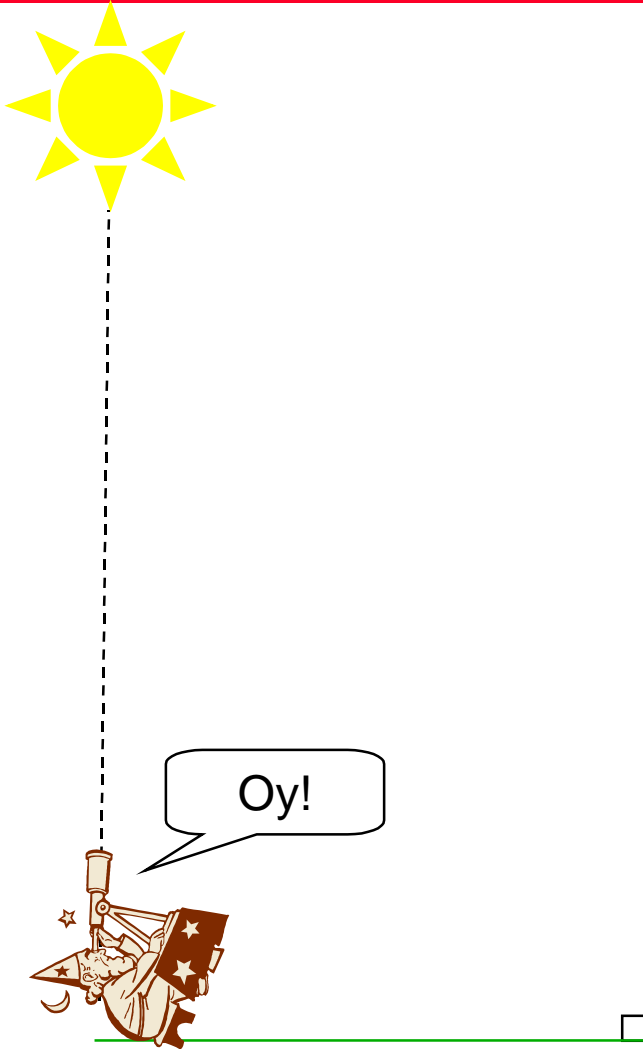
- If difference is less than 10% (“closed track”), use average
- If difference is greater than 10% (“open track”), don’t count



$$\text{Error} = 100 * \frac{(\text{Estimate 1} - \text{Estimate 2})}{(\text{Estimate 1} + \text{Estimate 2})}$$

$$\text{Altitude} = (\text{Estimate 1} + \text{Estimate 2}) / 2$$

# Implementation details



- **Minimum error when measured angles are near 45 degrees. The sine function doesn't change much near 90 degrees, and the tangent of 90 degrees is infinity!**
- **To avoid looking into the sun, it is best to have the baseline run East-West, and to be offset to the south of the pads**